Fast**National University of Computer & Emerging Sciences, Karachi  
Fall-2017 CS-Department  
Final Exam  
27th December 2017, 9:00 am – 12noon**

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| **Course Code: CS301** | **Course Name: Theory of Automata** | |
| **Instructor Name / Names: M. Shahzad** | | |
| **Student Roll No:** | | **Section No:** |

Instructions:

* Attempt all questions.
* All questions carry different marks. But equally distributed in all parts.
* It is advisable to go through the paper once before starting with the first question.
* Exam is a closed books and closed notes.
* Don’t use pencil , write in dark blue or black pen.

**Q 1a) Decide if the following statements are TRUE or FALSE:**  **[7.5 points = 15\*0.5 points]**

|  |  |
| --- | --- |
| 1) A production of the form non-terminal-> non-terminal is called a dead Production. | T/F |
| 2) Semi-word is a string having some terminals and one non-terminal at the right of string. | T/F |
| 3) Two FAs are equivalent if they have same no. of states. | T/F |
| 4) There exist exactly two different derivations in an ambiguous CFG for a word. | T/F |
| 5) Regular languages are closed under Union, Concatenation and Kleene star. | T/F |
| 6) CFG may also represent a regular language. | T/F |
| 7) PDA is stronger than FA. | T/F |
| 8) There always exist an FA for each PDA. | T/F |
| 9) If, two strings x and y, defined over Σ, are run over an FA accepting the language L, then x and y are said to belong to the same class if they end in the same state, no matter that state is final or not. | T/F |
| 10) The context free grammar *S->a|ab|SS|Sb* is ambiguous. | T/F |
| 11) The class of non-regular languages is closed under complementation. | T/F |
| 12) The concatenation of the two CFGs is not context free. | T/F |
| 13) The class of the non-context free languages is closed under complementation. | T/F |
| 14) If L1 and L2 are context free, then the language L1 - L2 must be contextfree. | T/F |
| 15) If L1 is context free and L2 is regular then the language L1 - L2 must be contextfree. | T/F |

**Q1b) Choose the best option in each of the following statements:**

**[7.5 points = 15\*0.5 points]**

|  |  |
| --- | --- |
| 1) Grammatical rules which do not involve the meaning of words are called ---------------   1. Semantics 2. Syntactic 3. Both a and b 4. None of given | 2) Grammatical rules which involve the meaning of words are called ---------------   1. Semantics 2. Syntactic 3. Both a and b 4. None of given |
| 3) The PDA is called non-deterministic PDA when there are more than one out going edges from……… state   1. START or READ 2. POP or REJECT 3. READ or POP 4. PUSH or POP | 4) S → aXb|b, XaX → aX|bX|Λ The given CFG generates the language in English \_\_\_\_\_\_\_\_\_\_   1. Beginning and ending in different letters 2. Beginning and ending in same letter 3. Having even-even language 4. None of given |
| 5) The symbols that can’t be replaced by anything are called -----------------   1. Productions 2. Terminals 3. Non-terminals 4. All of above | 6) The symbols that must be replaced by other things are called \_\_\_\_\_\_\_\_\_\_   1. Productions 2. Terminals 3. Non-terminals 4. None of given |
| 7) The grammatical rules are often called\_\_\_\_\_\_\_\_\_\_\_\_\_   1. Productions 2. Terminals 3. Non-terminals 4. None of given | 8) The language generated by that CFG is regular if \_\_\_\_\_\_\_\_\_   1. No terminal → semi word 2. No terminal → word 3. Both a and b 4. None of given |
| 9) The terminals are designated by \_\_\_\_\_\_\_\_ letters, while the non-terminals are designated by \_\_\_\_\_\_\_\_ letters.   1. Capital, bold 2. Small, capital 3. Capital, small 4. Small, bold | 10) The language generated by \_\_\_\_\_\_\_\_\_\_ is called Context Free Language (CFL).   1. FA 2. TG 3. CFG 4. TGT |
| 11) Identify the TRUE statement:   1. A PDA is non-deterministic, if there are more than one READ states in PDA 2. A PDA is never non-deterministic 3. Like TG, A PDA can also be non-deterministic 4. A PDA is non-deterministic, if there are more than one REJECT states in PDA | 12) Which statement is true?   1. The tape of turing machine is infinite. 2. The tape of turing machine is finite. 3. The tape of turing machine is infinite when the language is regular 4. The tape of turing machine is finite when the language is nonregular. |
| 13) The productions of the form nonterminal → one nonterminal, is called \_\_\_\_\_\_\_\_\_   1. Null production 2. Unit production 3. Null able production 4. None of given | 14) For language L defined over {a, b}, then L partitions {a, b}\* into …… classes   1. Infinite 2. Finite 3. Distinct 4. Non-distinct |
| 15) Σ = {a,b} Productions  S→XaaX X→aX  X→bX  X→Λ  This grammar defines the language expressed by\_\_\_\_\_\_\_\_\_\_\_   1. (a+b)\*aa(a+b)\* 2. (a+b)\*a(a+b)\*a 3. (a+b)\*aa(a+b)\*aa 4. (a+b)\*aba+b)\* |  |

**Q2) Provide short answers to each of the following questions:** **[10 points = 5\*2 points]**

a) Every subset of a regular language is regular.

b) Let L4 = L1L2L3. If L1 and L2 are regular and L3 is not regular, it is possible that L4 is regular.

c) Let L1 = L2 ∩ L3. Show values for L1, L2, and L3, such that L1 is context-free but neither L2 nor L3 is.

d) Let L1 = L2 ∩ L3. Show values for L1, L2, and L3, such that L1 is context-free but neither L2 nor L3 is.

e) Let L4 = L1L2L3. If L1 and L2 are regular and L3 is not regular, it is possible that L4 is regular.

**Q3) Following problems are related to CFG & CNF:**  **[10 points=5\*2 points]**

a) Show a context-free grammar that generates L = {w ∈ {a, b}\* : the first, middle, and last characters of w are identical}.

b) Convert the following grammar (over the alphabet {a, b, c, d}) to the Chomsky normal form.

**S → aSd | T**

**T → bTc | ɛ.**

c) Consider the following grammar *G*:

***S* → 1 *S* 1 | *T***

***T* → 1 *X* 1 | *X***

***X* → 0 *X* 0 | 1**

(i)What are the first four strings in the lexicographic enumeration of *L*(*G*)?

(ii)Show that *G* is ambiguous.

d) Let G be the context free grammar:

S →ASB | ɛ A →S | aAS | ɛ B →SbS | A | bb

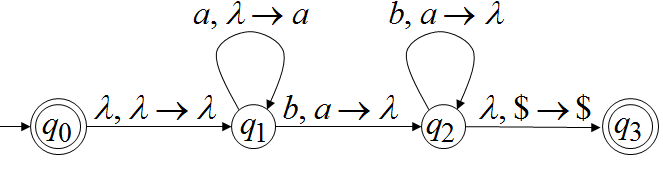
(i) Find a grammar G1 which has no ɛ -rule and L(G1) = L(G) – { ɛ }. [5pts]

(ii) Find a grammar G2 which is equivalent to G1 and has no unit productions

e) Define components of CFG

**Q4) All of the follwing problems are related to PDA:** **[10 points=5\*2 points]**

a) Process the string ***aaabbb***and fill the table with all possible values of State, STACK and Tape using following NPDA:



|  |  |  |
| --- | --- | --- |
| **STATE** | **STACK** | **TAPE** |
| qo | $ | aaabbb |
|  |  |  |
|  |  |  |
|  |  |  |

**Note: Highlights the current tape symbol with underline**

b) Suppose the PDA



has the following transition function:



Starting from the initial ID (*q, w, Z0*), show all the reachable ID's when the input *w* is:

i) 01

ii) 0011

c): Convert the following expression grammar into a PDA:

***I → a | b | Ia | Ib | I0 | I1***

***E → I | E \* E | E + E | (E)***

d) Construct PDA of the given language:



e) Write down the capabilties of PDA which cannot be achieved by CFG.

**Q5) Attempt all following related to TM:**  **[10 points = 2 \* 5 points]**

a): Prove that the following function is computable.

f(n)=n+2.

We know that if any function is computable, then there exists a Turing Machine for it. So, it will be sufficient to construct a TM to prove any function is computable.

TM behaves as follows:

q0IIIB ├\* IIIq0B ├IIIIq1B ├\* IIIIIBhB

b) Construct a Turing Machine accepting a language of palindrome over {a,b}\* with each string of even length.